

Result $d = D - 2\epsilon$

$$P = n_1 + \dots + n_{N-1} + 2r$$

$$(T_N) \underbrace{0 \dots 0}_{2r} \underbrace{1 \dots 1}_{n_1} \underbrace{2 \dots 2}_{n_2} \dots = H^{2\epsilon} \frac{(-1)^{N+P-r}}{2^r} e^{\gamma\epsilon} \Gamma(N - \frac{d}{2} - r) \int_0^1 dx_1 \dots dx_N \delta(1 - \sum_i x_i) \frac{x_1^{n_1} \dots x_{N-1}^{n_{N-1}}}{(\Delta)^{N - \frac{d}{2} - r}}$$

Special cases:

if $d = 4 - 2\epsilon$

$$A_{0 \dots 0}^{2r}(m_0) = H^{2\epsilon} \frac{(-1)^{1+r}}{2^r} e^{\gamma\epsilon} \Gamma(1 - \frac{d}{2} - r) \left(\frac{1}{\Delta}\right)^{1 - \frac{d}{2} - r} \quad \Delta = m_0^2 - i\epsilon$$

$$B_{0 \dots 0}^{2r} \underbrace{1 \dots 1}_{n_1} (p^2, m_0, m_1) = H^{2\epsilon} \frac{(-1)^{2+r+n_1}}{2^r} e^{\gamma\epsilon} \Gamma(2 - \frac{d}{2} - r) \int_0^1 dx \frac{x^{n_1}}{(\Delta)^{2 - \frac{d}{2} - r}}$$

where $\Delta = p^2 x^2 + (-p^2 + m_1^2 - m_0^2)x + m_0^2 - i\epsilon$

$$C_{0 \dots 0}^{2r} \underbrace{1 \dots 1}_{n_1} \underbrace{2 \dots 2}_{n_2} (p_1^2, q^2, p_2^2; m_0, m_1, m_2)$$

$$= H^{2\epsilon} \frac{(-1)^{3+r+n_1+n_2}}{2^r} e^{\gamma\epsilon} \Gamma(3 - \frac{d}{2} - r) \int_0^1 dy \int_0^{1-y} dz \frac{y^{n_1} z^{n_2}}{(\Delta)^{3 - \frac{d}{2} - r}}$$

where $\Delta = p_1^2 y^2 + p_2^2 z^2 + (-q^2 + p_1^2 + p_2^2)yz + (-p_1^2 + m_1^2 - m_0^2)y + (-p_2^2 + m_2^2 - m_0^2)z + m_0^2 - i\epsilon$

and $q^2 = (p_2 - p_1)^2$

$$3 - \frac{4-2\epsilon}{2} - r = 1 + \epsilon - r$$

$$D_{\substack{0 \dots 0 \\ 2r}} \substack{1 \dots 1 \\ n_1} \substack{2 \dots 2 \\ n_2} \substack{3 \dots 3 \\ n_3} = \mu^{2e} \frac{(-1)^{4+r+n_1+n_2+n_3}}{z^r} e^{2e} \Gamma(2+e-r)$$

$$\int_0^1 dx \int_0^{1-x} dy \int_0^{1-x-y} dz x^{n_1} y^{n_2} z^{n_3} \Delta(x, y, z)^{-2-e+r}$$

$$\Delta(x, y, z) = ax^2 + by^2 + cz^2 + dxy + exz + fyz + gx + hy + iz + j$$

$$a = p_1^2 = S_1$$

$$b = p_2^2 = S_{12}$$

$$c = p_3^2 = S_4$$

$$d = 2p_1 p_3 = (S_{12} + S_1 - S_2)$$

$$e = 2p_1 p_2 = (-S_{23} + S_1 + S_4)$$

$$f = 2p_2 p_3 = (S_{12} + S_4 - S_2)$$

$$g = (-p_1^2 + m_1^2 - m_0^2) = -S_1 + m_1^2 - m_0^2$$

$$h = (-p_2^2 + m_2^2 - m_0^2) = -S_{12} + m_2^2 - m_0^2$$

$$i = (-p_3^2 + m_3^2 - m_0^2) = -S_4 + m_3^2 - m_0^2$$

$$j = m_0^2 - iE = m_0^2 - iE$$